An Ultra-thin Monolithic XY Nanopositioning Stage Constructed from a Single Sheet of Piezoelectric Material

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Abstract—The article describes an XY nanopositioning stage constructed from flexures and actuators machined into a single sheet of piezoelectric material. Ultrasonic machining is used to remove piezoelectric material and create electrode features. The constructed device is 0.508 mm thick and has a travel range of 8.6 $\mu$m in the X and Y axes. The first resonance mode occurs at 597 Hz which makes the device suitable for a wide range of standard nanopositioning applications where cost and size are considerations. Experimental atomic force microscopy is performed using the proposed device as a sample scanner.

I. INTRODUCTION

Nanometer resolution positioning systems are used extensively in applications where a sample, probe, or substrate is scanned or statically positioned [1]. Scanning applications include atomic force microscopy [2]–[7] and data storage [8]; while non-scanning applications include nanofabrication [9], [10], cell surgery [11], and precision optics [12]. Nanopositioning systems typically use piezoelectric actuators and a feedback system to eliminate actuator non-linearity and reject external disturbances [13]–[15].

The first common nanopositioning systems were based on the piezoelectric tube scanner, which was famously used to demonstrate the scanning tunneling microscope in 1986 [16]. These monolithic tube structures are economical and can provide sub-atomic resolution. However, to achieve a useful scan-range, for example 50 $\times$ 50 $\times$ 10 $\mu$m (X $\times$ Y $\times$ Z), they must be physically long (50 mm) and therefore suffer from low-resonance frequencies and significant cross-coupling between the lateral and vertical axes [17]–[19].

To improve the speed and reduce out-of-axis motion, flexure-based nanopositioners were developed. These devices use piezoelectric actuators to drive a moving platform guided by metal flexures [20]–[24]. The high flexural stiffness dramatically reduces cross-coupling and allows a much larger payload than monolithic devices. However, flexure-based nanopositioners are considerably more costly, heavier, and bulkier than monolithic devices.

This article describes a new class of nanopositioning system that is monolithic in structure but also incorporates flexural motion guidance. Previous monolithic nanopositioners were primarily extruded; however, the proposed device is constructed by removing material from a piezoelectric sheet by ultrasonic machining. By adding surface electrodes, active flexures are formed that generate displacement and guide the resulting motion. The stiffness, resonance frequencies, and travel range can be varied by changing the geometry of the flexures and electrode coverage. Furthermore, multiple different devices can be constructed on the same sheet of material, for example, multiple two-axis scanners with differing travel ranges and resonance frequencies.

In this work, a 0.508 mm thick sheet is used to create an XY nanopositioning stage than can translate an $18 \times 18$ mm load by up to 10 $\mu$m. This device is an order of magnitude thinner than the nearest comparable nanopositioner design. The small size allows a new range of applications in optomechanics, atomic force microscopy, and particularly, scanning electron microscopy where the load-lock area may be less than 5 mm in height [25]. The low cost is also a significant advantage which may enable the cost of scanning probe microscopes to be significantly reduced.

A. Contributions

A preliminary version of this work was presented at the IEEE conference on Advanced Intelligent Mechatronics in 2016 [26]. In this work, the electrode features were created using a Nitric acid printing process; however, this article describes an ultrasonic milling process for both bulk material removal and surface electrode patterning. This was found to be superior. Other major revisions since the conference article include:

- Revision of the boundary conditions to match the experimental bonded condition. This provides much closer agreement between FEA and experimental results.
- The voltage range is reduced to -200 V to +500 V to match the safe operating range of the material.
- Time-domain and frequency-domain characterization is performed in all three axes, including cross-coupling.
- Atomic force microscopy is demonstrated in Section VII
- The maximum payload, cross-coupling, and robustness is analyzed in Section VIII.

In the following section, the overall design is described, followed by an in-depth analysis of the vertical stiffness and resonance frequency in Section III. Finite element simulations are presented in Section IV followed by a description of the fabrication process in Section V. Experimental results and a demonstration of atomic force microscopy are presented in Sections VI and VII. Practical considerations and conclusions are then discussed in Sections VIII and IX.

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II. DESIGN

As illustrated in Figure 1, the proposed design consists of a thin piezoelectric sheet with a number of cuts designed to create parallel beams that drive a central platform. The entire bottom surface is covered by a single grounded electrode. A simplified diagram of the structure and top electrode is shown in Figure 2. Assuming that the poling vector is in the +Z direction, a positive voltage applied to the electrode will cause the beam to expand and displace the central platform away from the positive voltage. For example, when a positive voltage is applied to the top surface will cause the beam to expand and displace the central platform away from the positive voltage. To develop the greatest deflection and force, the +Vx and -Vx electrodes are driven in a push-pull configuration as described in Figure 2.

To model the motion of the platform, a single beam of length \( L_f \) is first considered. Assuming that the bottom surface is grounded and that the poling vector is in the +Z axis, the free elongation \( \Delta L \) can be derived from the standard piezoelectric equations [27]

\[
\Delta L = L_f d_{31} E = \frac{L_f d_{31}}{t} V,
\]

where \( d_{31} \) is the piezoelectric strain constant, \( L_f \) is the length, \( E \) is the electric field, \( t \) is the thickness, and \( V \) is the applied voltage.

Although piezoelectric actuators are typically modeled as displacement actuators as described above, this simplification is only valid when there is no load force or interconnected structure. For structures with interconnected actuators, the use of force and stiffness is more appropriate. By beginning with the stress-charge form of the piezoelectric constituent equations [27], the generated force and associated stiffness can be derived,

\[
F_a = d_{31} k_a V, \quad k_a = \frac{c^E A}{L_f},
\]

where \( c^E \) is the Young’s modulus of elasticity, \( A \) is the cross-sectional area, and \( k_a \) is the internal stiffness derived by considering the axial mechanics of a bar. This model structure allows multiple parallel actuators to be modeled by a summation of the forces and stiffness.

If the electrodes on opposite sides are driven asymmetrically in a push-pull configuration, the total force is doubled. Therefore with \( N \) beams on either side, the total force and stiffness is

\[
F_a^* = 2N d_{31} k_a V, \quad k_a^* = 2N \frac{c^E A}{L_f}
\]

The total deflection can be derived from \( \Delta L = F_a^*/k_a^* \), which reduces to \( \Delta L = L_f d_{31}/t V \), which is identical to the free extension of a single beam.

In this work, the flexure length is chosen to be \( L_f = 17 \) mm with a thickness of \( t = 0.5 \) mm. Therefore, the predicted deflection is

\[
\Delta L = \frac{L_f d_{31}}{t} V = V \times 6.5 \text{ nm/V}.
\]

Since the maximum applied voltage is 700 V peak-to-peak, the predicted displacement range is 4.6 \( \mu \)m peak-to-peak. If the maximum positive voltage is extended to +1000 V, the predicted displacement is increased to 7.8 \( \mu \)m peak-to-peak.

III. MODELING

In this section the effective stiffness, mass, and resonance frequency in the vertical (Z) direction is derived. Due to the planar design of the proposed device, the vertical resonance modes dominate the frequency response. Therefore, it is of particular interest to understand the first resonance mode and be able to predict how it is affected by factors such as geometry, external forces, and additional mass.

A. Effective Stiffness in Z Axis

The strain energy method and Castigliano’s second theorem [28] are used to derive the effective stiffness of each flexure. Castigliano’s second theorem is a simple and intuitive technique that allows the calculation of elastic bodies’ deformation...
under external and reaction loadings acting at that location [28], [29]. This method has been widely used in designing flexure-guided nanopositioners [24], [30]. Using Castigliano’s second theorem, the vertical displacement \( u_z \) of the beam flexure in Fig. 3 is defined as [24], [28], [30]

\[
u_z = \left( \frac{L_f^3}{3EI_y} \right) F_z + \left( \frac{L_f^2}{2EI_y} \right) M_y,
\]

where \( L_f \) is the length of the flexure, \( E \) is the Young’s modulus, \( I_y = \text{ht}^3/12 \). Under the boundary condition of a fixed-guided beam, the resultant moment \( M_y \) at the guided end of the beam due to the applied load \( F_z \) at that point is \( M = -F_z L_f/2 \). Note that \( F_z \) is actually applied at the center of the platform as shown in Fig. 3. Therefore, the resultant moment \( M_y \) at the guided end of the beam is

\[
M_y = \frac{F_z L_p}{2} - \frac{F_z L_f}{2} = \frac{F_z}{2} (L_p - L_f),
\]

where \( L_p \) is the length of the platform. Substituting Eq. (6) into Eq. (5) yields

\[
u_z = F_z \left[ \frac{L_f^3}{3EI_y} - \frac{L_f^2}{4EI_y} (L_p - L_f) \right].
\]

Hence, the stiffness of the flexure in the Z-direction is

\[
k_z = \frac{F_z}{u_z} = \left[ \frac{L_f^3}{3EI_y} - \frac{L_f^2}{4EI_y} (L_p - L_f) \right]^{-1}.
\]

Since all flexures are arranged in parallel, the total stiffness of the monolithic nanopositioner is

\[
K_z = N k_z,
\]

where \( N \) is the number of flexures.

### B. Effective Mass and Resonance frequency

The effective mass of the flexure \( m_{eff} \) is calculated using the Rayleigh’s principle [31],

\[
m_{eff} = \rho A \int_0^l \left( \frac{z(x)}{z_{max}} \right)^2 \, dx,
\]

where \( \rho \) is the material density, \( A = \text{ht} \) is the cross-sectional area of the flexure, \( z(x) \) is the shape function (vibration amplitude) of the flexure, and \( z_{max} \) is the maximum displacement of the flexure along the Z-direction. The shape function for a fixed-guided beam with \( F_z \) applied at its guided-end is

\[
z(x) = -\frac{F_z}{12EI_y} (L_f - x)^2 (L_f + 2x).
\]

The maximum displacement is \( z_{max} = -F_z L_f^3/(12EI_y) \). Thus,

\[
z(x) = \frac{(L_f - x)^2 (L_f + 2x)}{L_f^3}.
\]

Substituting Eq. (12) into Eq. (10) and solving the integration gives

\[
m_{eff} = \frac{13}{35} \rho AL_f = \frac{13}{35} m_f,
\]

where \( m_f \) is the mass of each flexure. Knowing the mass of the platform \( m_p = \rho L_p^2 t \), the effective mass of the nanopositioner can then be obtained by

\[
M_e = Nm_{eff} + m_p.
\]

The resonance frequency in the Z-direction can be derived as

\[
f_{res} = \frac{1}{2\pi} \sqrt{\frac{K_z}{M_e}}.
\]

Substituting all the corresponding parameter values from Table I into Eqs. (9), (14) and (15), the resonance frequency is \( f_{res} = 425.6 \text{ Hz} \).
IV. Simulation

A finite-element (FE) model of the piezoelectric nanopositioner was generated using ANSYS Workbench. Boundary conditions of the model are shown in Fig. 4 where the displacement of all four edges are fixed. Meshing was generated initially using the automesh tool. It was then refined manually to obtain more accurate results. The piezoelectricity of the nanopositioner is modeled using the ANSYS Coupled Field Physics ACT (Application Customization Toolkit) extension. Table II lists the piezoelectric coefficients in stress form $e_{ij}$ and the relative permittivity $\varepsilon_r = \varepsilon^r / \varepsilon_0$ required for constructing the piezoelectric body in ANSYS. The polarization vector of the piezoelectric material is in the +Z direction. The maximum displacement of the X-axis was simulated by applying +500 V and -200 V, as shown in Fig. 4. The simulated displacement was $\pm 3 \mu m$ in both lateral axes.

The resonance modes were simulated using the modal analysis module of ANSYS Workbench. The first four resonance modes are illustrated in Fig. 5. The vertical resonance mode appears at 530.9 Hz which is in close agreement with the analytical result, i.e. 425.6 Hz.

### Table II

<table>
<thead>
<tr>
<th>Piezoelectric coefficient, $C/m^2$</th>
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<tbody>
<tr>
<td>$e_{31}$</td>
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<tr>
<td>$e_{33}$</td>
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<td>$e_{15}$</td>
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<tr>
<th>Relative permittivity, $\varepsilon_r = \varepsilon^r / \varepsilon_0$</th>
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<td>$\varepsilon_{11}$</td>
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<tr>
<td>$\varepsilon_{33}$</td>
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<tr>
<th>Piezoelectric constant, $pm/V$</th>
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<tbody>
<tr>
<td>$d_{31}$</td>
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V. Fabrication

The nanopositioner was fabricated from a monolithic sheet of PZT-5A with sputter coated 5-µm Nickel electrodes. The sheet measures 72.3×72.3×0.508 mm and was obtained from Piezo Systems Inc. (T120-A4E-602). A number of methods for direct machining were attempted such as laser cutting, CNC milling, and ultrasonic machining. Ultrasonic machining was the slowest method but provided excellent cut quality with no thermal damage of the material or electrodes. The working tool was a sintered diamond core drill, vibrating at 21 kHz and rotating at 8000 rpm. The cutting depth was 0.1 mm per pass. Using these machining parameters, precise lines could be milled through the PZT without causing significant heating or inducing the formation of fractures. The final shape and critical dimensions are illustrated in Fig. 6.

The electrodes were created with a single-pass cutting depth of 25 µm. Photolithography and direct acid printing were also trialed [26] but direct machining was found to produce sufficiently fine features without the need for chemical etching.

VI. Experimental Results

The experimental setup consists of the nanopositioner mounted on a base as pictured in Figure 7. For safety reasons, the device is mounted upside-down so that the top electrode is grounded and the high-voltage electrodes are inaccessible. The
motion in each axis is measured simultaneously with a Polytec MSA-3D interferometer. A comparison of the analytical, finite element, and experimental performance is listed in Table III.

To evaluate the travel range, both sides were driven asymmetrically with a 1-Hz sinusoidal voltage from -200 V to +500 V. Note that +500V is only half the positive voltage range but was chosen for safety reasons. The resulting lateral deflection is plotted in Figure 8 which shows a travel range of 8.6 µm in X and 10.8 µm in Y. The X and Y axis travel range were both slightly higher than the predicted range, which was 4.6 µm analytically and 6.0 µm by FEA. The difference between the predicted and experimental range is presumed due to uncertainty in $d_{31}$ and the magnitude of the applied voltage. Piezoelectric constants are quoted for small-signals, however, the non-linearity of piezoelectric material results in significant differences when the full voltage range is utilized. The change in sensitivity versus voltage can be observed in the hysteresis plot in Figure 8, which is typical of PZT-5A material.

In Figure 9 the X and Y-axis frequency responses exhibit a relatively constant response over a wide frequency range. However, the maximum useful frequency is limited by the first vertical mode measured at 597 Hz. This value compares well with the finite element simulation (531 Hz) and the analytical prediction (426 Hz). The discrepancy is due to the the 2-mm glue strip on the experimental system which slightly stiffens the structure. The small, low-frequency peaks are thought to be the resonance modes of the wires between the electrodes and connector. These wires have a significant mass relative to the structure, so their resonance modes can be seen in the response. In future, the electrical wiring will be integrated into the outside support structure of the device, which will eliminate wiring and the associated resonances.

<table>
<thead>
<tr>
<th></th>
<th>Analytical</th>
<th>FEA</th>
<th>Experimental</th>
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</thead>
<tbody>
<tr>
<td>X Travel (700 Vp-p)</td>
<td>4.6 µm</td>
<td>6.0 µm</td>
<td>8.6 µm</td>
</tr>
<tr>
<td>1st Resonance Freq</td>
<td>426 Hz</td>
<td>531 Hz</td>
<td>597 Hz</td>
</tr>
<tr>
<td>Maximum Payload</td>
<td>21 g</td>
<td>19 g</td>
<td>N/A</td>
</tr>
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</table>

VII. ATOMIC FORCE MICROSCOPE IMAGING

To demonstrate the application of the proposed nanopositioner, the experimental setup in Figure 7 was used to obtain an 8×8 µm image of a Budget Sensors HG-100MG calibration grating. The grating is a rectangular array with a 5-µm period and 100-nm height. A contact-mode ContAl-G cantilever with a resonance frequency of 13 kHz was used to probe the sample. The grating was imaged in constant-force contact-mode using a Nanosurf EasyScan2 AFM mounted on top of
the nanopositioner. The contact force was regulated at 30 nN.

The calibration grating was placed on the central platform of the nanopositioner. To move the grating in a raster pattern, the X-axis of the nanopositioner was driven with a 0.5-Hz triangular waveform, and the Y-axis was driven with a ramp signal. The vertical signal of the AFM head was recorded and used to construct the image in Figure 10. The image processing included the removal of a plane from image, which results from tilting of the sample and cross-coupling between the lateral and vertical axis. The effect of hysteresis can be observed in the image as the feature edges are not perfectly straight.

Fig. 9. The measured frequency responses from the applied voltage to the X, Y, and Z axis deflection (in µm/V). Hyx refers to the frequency response from the X-axis input to the Y-axis deflection, and so on.

VIII. DISCUSSION

In Figure 10, the monolithic stage is suitable for high-resolution AFM imaging despite the relatively high cross-coupling between the lateral axes (-20 dB or 10%), and between the lateral and vertical axes (-25 dB or 6%). By comparison, a typical commercial nanopositioner would have a cross-coupling better than -30 dB (3%). Although the lateral cross-coupling is significant, this is not evident in the image since the artefact is image rotation. The vertical cross-coupling adds a sloping plane to the image, which is automatically removed in standard AFM image processing. For other applications such as lithography, the cross-coupling would need significant improvement. Current research involves the use of a 3-axis closed-loop control and improvements to the mechanical design which reduce the lateral stiffness and increase the vertical stiffness.

The maximum payload is determined by the stress $\sigma_f$ in the piezoelectric flexures, which was derived in reference [32],

$$\sigma_f = \frac{0.15F_zL_f}{ht^2},$$  \hspace{1cm} (16)

where $\sigma_f$ is the stress, $F_z$ is the vertical force, $L_f$ is the flexure length, $h$ is the flexure width, and $t$ is the thickness. The maximum tensile strength of PZT-5A is 11 MPa [33], therefore, the maximum vertical force is 2.1 N. To maximize the service life, it is desirable to avoid exceeding 10% of the maximum tensile stress, which corresponds to a vertical force is 0.21 N and a maximum payload mass of 21 g. Using finite element analysis, the maximum force and payload was found to be of 1.9 N and 19 g respectively.

Typical metal-flexure nanopositioners have a maximum payload on the order of 500 g, which is 25 times greater than the proposed design; however, they are also typically 25 times thicker. The maximum 2.1 N vertical force of the monolithic stage means that it is less robust than a standard nanopositioner; however, this may be an acceptable trade-off given the simplicity, low-cost, and small dimensions.

Present research includes laminating multiple piezo-layers together to improve the vertical stiffness, robustness, and maximum payload; however, it is accepted that this detracts from the simplicity of the single-layer structure.

IX. CONCLUSIONS

This article proposes a new method for designing and fabricating nanopositioning systems from a single sheet of
piezoelectric material. Ultrasonic milling was used to construct a two-axis nanopositioner from active flexures and electrodes. Analytical and finite element models were derived which closely match the experimental response. A full-scale range of 8.6-μm was achieved with a resonance frequency of 597 Hz.

The completed nanopositioner is only 508 μm in thickness which is an order-of-magnitude thinner and lighter than the state-of-the-art. The proposed fabrication method has the potential to dramatically reduce the size and cost of many other positioning systems including rotational stages, vertical positioners, and mirror scanners.

Current focus is on the integration of closed-loop sensors and the development of more complex geometries to improve the travel range and provide additional degrees of freedom such as rotation and vertical motion.

REFERENCES


Yuen Kuan Yong received the Bachelor of Engineering degree in Mechatronics Engineering and the Ph.D degree in mechanical engineering from The University of Adelaide, Australia, in 2001 and 2007, respectively. She is currently an Australian Research Council DECRA Fellow with the School of Electrical Engineering and Computing, The University of Newcastle, Australia. Her research interests include nanopositioning systems, micro-cantilevers, high-speed atomic force microscopy, and miniature robotics. In 2014, Dr Yong received the University of Newcastle Vice-Chancellor’s Awards for Research Excellence, and the Pro Vice-Chancellors Award for Excellence in Research Performance. She is an Associate Editor for the IEEE/ASME Transactions of Mechatronics, and Frontiers in Mechanical Engineering.